Design and MultiPlierless Realization of ECG- Based Gaussian Wavelet Filter with Lattice Structures

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Abstract

In this paper, the Gaussian function is selected as a mother wavelet function and utilized in the design of some corresponding filter banks. With a 1st derivation of the Gaussian function, a similar shape to QRS complex part of the ECG is achieved.It can be used for QRS feature extraction.Using thesymmetry property of the mother wavelet function, the designed FIR wavelet filter banks can be realized in highly-efficient lattice structures which are easy to implement. The resulting lattice structures reduces the number of filter banks coefficients and this reduces, in turn the number of multiplications and improves the filter banks efficiencies as it reduces the number of computations performed. Hardwarely, this leads to less-complex implementations. The resulting quantized multiplier values also lead to a multiplierless realization for such wavelet filter banks.

Keywords: ECG,Wavelet and scaling functions, Filter banks, Lattice structures, Multiplierless realization.

التصميم والتحقيق بلا مضارب لمرشح مويجي نوع دالة كاوسبإعتمـاد إشارة ECGوإستخدام الـهياكل المتشابكة

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الخلاصة

في هذا البحث، تم إختيار دالة كاوس كدالة أم مويجيةوإستغلالها لتصميم بعض أجراف مرشحات مقابلة. وبمجرد أن تجرى عملية إشتقاق من المرتبة الاولى لدالة كاوس، سنحصل على شكل مماثل لجزء QRS المعقّد في إشارة ECG، والتي يمكن أن تستعمل لإستخلاص ميزّات QRS.وإعتماداً علىخاصية التناظر لهذه الدالة المويجة الأم، فإن المرشحات المصممة يمكن تحقيقها بهياكل متشابكة كفوءة جداً وسهلة البناء.الهياكل المتشابكة الناتجة تخفّض من عدد معاملات أجراف المرشحاتوهذا بدوره يخفّض عدد المضارب ويحسّن كفاءة أجراف المرشحات حيث أنه يخفّض عددالحساباتالمؤداة.وعلى صعيد المكونات المادية فإن هذا سيؤدّي إلى بناءات أقل تعقيّداً.إن قيم المضارب المكممة الناتجةستقود الى تحقيق بلا مضارب لأجراف المرشحات المويجية تلك.

I. Introduction

The electrocardiogram (ECG) is a time-varying signal that measures the electrical activity of the heart. The cardiac cycle begins with the P wave, which corresponds to the period of atrial depolarization in the heart. This is followed by the QRS complex, which is usually the most relevant (recognizable) feature of an ECG waveform. The T wave follows the QRS complex and corresponds to the period of ventricular repolarization(see Fig. 1)[1].
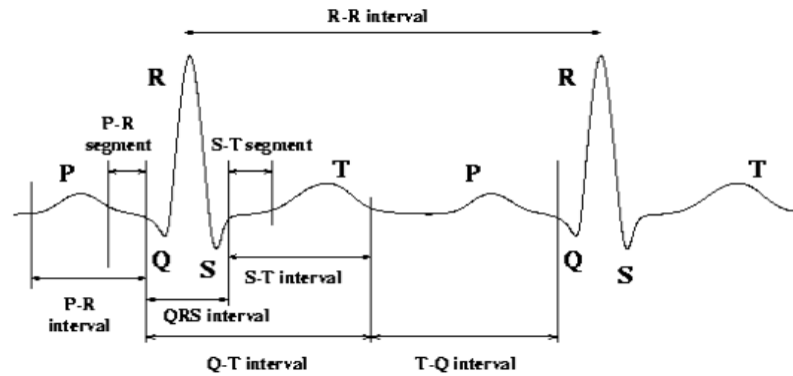

Fig.1 A Sample ECG Signal showing P-QRS-T Wave

The ECG signal represents the potential differencebetween two points on the body surface, versus time. Extracting the features from this signal has been found very helpful in explaining and identifying various cardiac arrhythmias[2].One of the most important ECG components is the QRS complex, which is associated with electrical ventricular activation[3],[4].

The ECG feature extraction system provides fundamental features (amplitudes and intervals) to be used in subsequent automatic analysis. In recent times, many techniques have been proposed to detect these features [5],[6]. Most of the previously proposed techniques for ECG signal analysis were based on time domain analysis. But this is not always adequate to study all the features of ECG signals. Therefore, the frequency representation of a signal is required. In recent years, many classifying methods which have been proposed including digital signal analysis, Fuzzy Logic methods, Artificial Neural Networks,Hidden Markov Model, Genetic Algorithm, Support vector Machines, Self-Organizing Map, Bayesian and other hybrid methods. Each of these approaches exhibits its own advantages and disadvantages [6].

The wavelet transform (WT) is one of several mathematical tools that is useful in the analysis and design of systems and signals. Its representation basically involves the decomposition of the signals in terms of small wave components called wavelets.Wavelet theory is employed in many fields and applications such as signal and image processing, communication systems, many other signal analysis and system control areas[7].The wavelet transform is an efficient technique for a non-stationary signal processing. ECG signal is one of the biosignals that is considered as a non-stationary one[8].There are many sets of wavelet bases that can be used to represent a signal. Each basis in a certain wavelet set is constructed form one function called the mother wavelet $\varphi(t)$. The multiresolutionanalysis of signals using wavelets involves two basic operations on the mother wavelet. These operations are the scale operation, and translation operation[7].

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The Gaussian function is perfectly local in both time and frequency domains and is indefinitely derivable. Any n^{th} order derivative of Gaussian function may be considered as a Wavelet Transform (WT). For cardiac signal characterization, a 1storder derivative Gaussian wavelet function is of interest [9]. The proposed design is obtained by simulating the 1st order derivative Gaussian system using a Gaussian system convolution stage with input signal $x(n)$ and differentiating the result. Due to linearity of system stages, the proposed digital-version system can be reordered as shown in Fig. 2 with ∇ as the 1st order backward difference operator.

Fig.2A proposed system with Gaussian function and a derivative stage.

The resulting wavelet filter banks can be realized in highly-efficient lattice structures which are easy to implement. The lattice structure reduces the number of coefficients and this, in turn reduces the number of multiplications and improves both; filter bank complexity and processing speed, as it reduces the number of computations performed [10]. Hardwarely, lattice structure leads to less-complex implementations.

Besides this introductory section, Section II of this paper contains the design of the FIR wavelet filter utilizing the Gaussian function as a mother wavelet function. Section III illustrates the lattice structure of such filter with a standard deviation $\sigma = 1$. A multiplierless realization of such structure is also proposed in this section.The lattice structure of the proposed filter with a standard deviation $\sigma = 2$ and its multiplierless realization are then described in section IV.The extracted features from some ECG signals representing a group of diseases in addition to the normal state are given in section V. Finally, Section VI concludes this paper.

II. Wavelet Filter Design

One of the functions in the wavelet techniques is the Gaussian function (see Fig. 3) that is defined by

$$\varphi(t) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\left(\frac{(t-m)^2}{2\sigma^2}\right)} \qquad \dots(1)$$

where $\varphi(t)$ is the Gaussian function in term the time t. σ is the standard deviation and$m$ is the center of the wave.
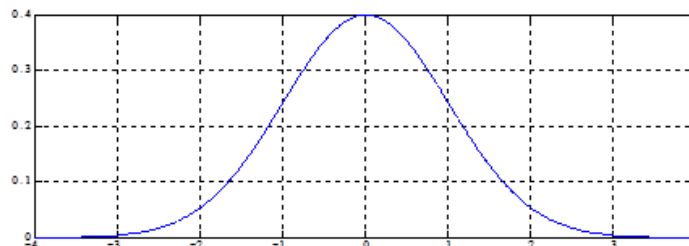

Fig. 3 The Gaussian function.

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In this paper, the Gaussian function is selected as a mother wavelet function. The 1st order derivative Gaussian function shown in Fig. 4, has a similar shape to QRS complex part of the ECG and can be used for QRS feature extraction. It is given by

$$\varphi'(t) = \frac{m-t}{\sigma^3\sqrt{2\pi}} e^{-\left(\frac{(t-m)^2}{2\sigma^2}\right)} \qquad \ldots(2)$$
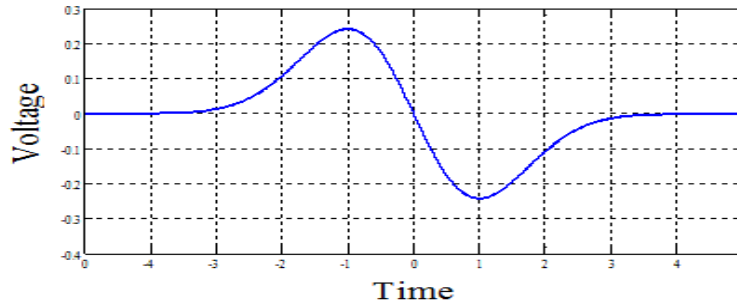

Fig. 4 The 1st derivative Gaussian function.

In order to design a corresponding FIR wavelet filter, the values of such FIR filter coefficients simulating the Gaussian response must be determined. To do so, the Gaussian function must be truncated in a way that assumes getting coefficients number depends upon standard deviation within the truncated function. To determine the values of these coefficients, the value of the standard deviation σ must be determined. The Gaussian function is approximately zero for $|t| > 4\sigma$. For example, $\varphi'(t, \sigma) < 0.0004$ for $|t| > 4$ σ. [11].

As shown in Fig. 3, since the response of designed FIR Gaussian wavelet filter stage of Fig. 2 possesses thesymmetry property, then the required number of filter coefficients (*i. e.,* multipliers) is $(1 + 4\sigma)$. Therefore, such FIR wavelet filter can be designed at various values of standard deviation, σ. Next section shows the design of FIR wavelet filters at$\sigma = 1$ and $\sigma = 2$.

III. Gaussian FIR Wavelet Filter with σ = 1
a) Lattice Structure

In the caseof σ = 1, the resulting filter response shown in Fig. 5, corresponds to the sampled version of the mother wavelet function in Fig. 3. It will have 9 coefficients with the following system function:

$$H(z) = h_0 + h_1 z^{-1} + h_2 z^{-2} + h_3 z^{-3} + h_4 z^{-4} + h_5 z^{-5} + h_6 z^{-6} + h_7 z^{-7} + h_8 z^{-8} \qquad \ldots(3)$$
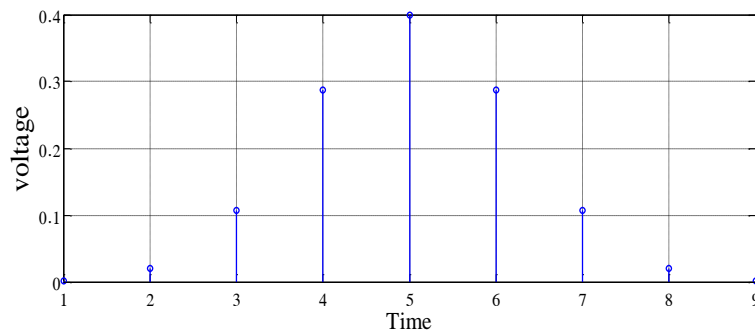

Fig. 5 Impulse response of the Gaussian filter stage.

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By the property of quadrature mirror filters (QMFs), $G(z) = H(-z)$, the system function $G(z)$ that corresponds to the scaling function can be written as

$$G(z) = h_0 - h_1 z^{-1} + h_2 z^{-2} - h_3 z^{-3} + h_4 z^{-4} - h_5 z^{-5} + h_6 z^{-6} - h_7 z^{-7} + h_8 z^{-8} \quad \dots (4)$$

The first design step is to find the polyphase matrix of the specified filter bank and a similar matrix of the proposed lattice structure. The block diagram of lattice structure of the proposed FIR wavelet filter is shown in Fig. 6, where ∇^2 represents the down sampled version of the 1st order backward difference operator. The filters' polyphase representations are expressed as functions of z, by

$$H_{even}(z^2) = h_0 + h_2 z^{-2} + h_4 z^{-4} + h_6 z^{-6} + h_8 z^{-8}$$

$$H_{odd}(z^2) = h_1 + h_3 z^{-2} + h_5 z^{-4} + h_7 z^{-6} \qquad \dots (5)$$

The down-sampled (by 2) form of equation (5) can be written as

$$H_{even}(z) = h_0 + h_2 z^{-1} + h_4 z^{-2} + h_6 z^{-3} + h_8 z^{-4} \qquad \dots (6)$$

$$H_{odd}(z) = h_1 + h_3 z^{-1} + h_5 z^{-2} + h_7 z^{-3}$$

Therefore,

$$H(z) = H_{even}(z) + z^{-1} H_{odd}(z)$$
And
$$G(z) = H_{even}(z) - z^{-1} H_{odd}(z) \qquad \dots (7)$$

with the following coefficients values:

$h_0 = h_8 = 0.0021, h_1 = h_7 = 0.0208, h_2 = h_6 = 0.1074, h_3 = h_5 = 0.2874$

and $h_4 = 0.3989$.
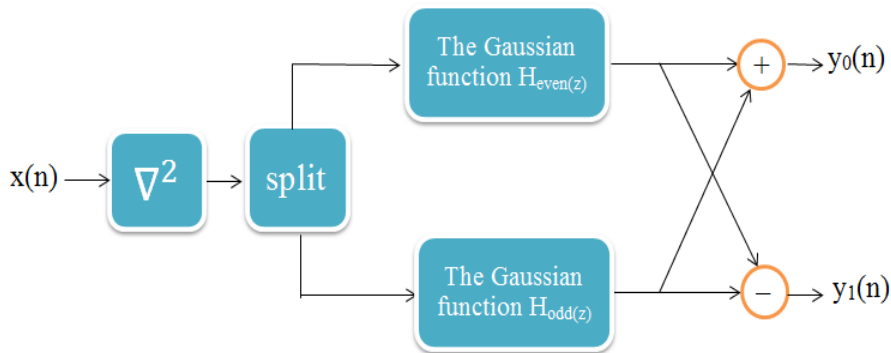
Fig. 6 Block diagram of lattice structure of the proposed FIR wavelet filter.

The values of coefficients can be scaled (by α) to give a maximum frequency response value equals to one, for the case of no-energy level variation during transformation. This value of α for [$|H(e^{j\omega})| \leq 1$] turns to be 0.81. Therefore, the new scaled coefficients values are as follows:

$h_0 = h_8 = 0.0017, h_1 = h_7 = 0.0169, h_2 = h_6 = 0.0870, h_3 = h_5 = 0.2328$ and $h_4 = 0.3231$.

After getting these coefficients, the design of the proposed FIR wavelet filter is accomplished. The magnitude and phase responses of $H(e^{j\omega})$ of the system function in equation (7), are shown in Fig. 7. The final overall lattice structure in Matlab simulation is shown in Fig. 8.
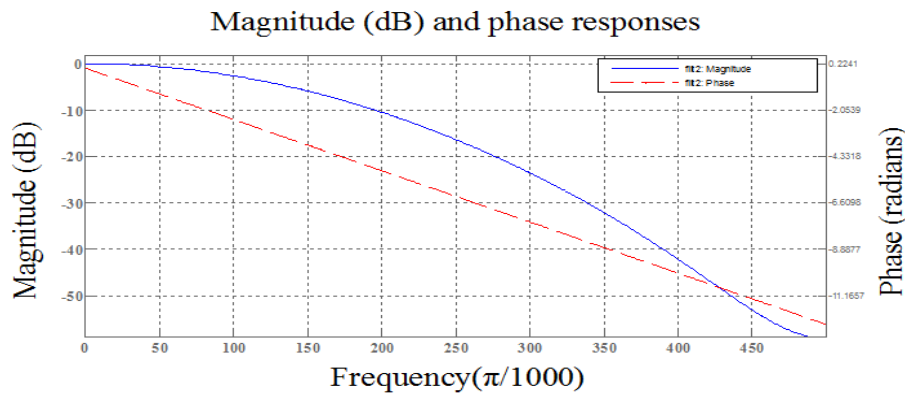

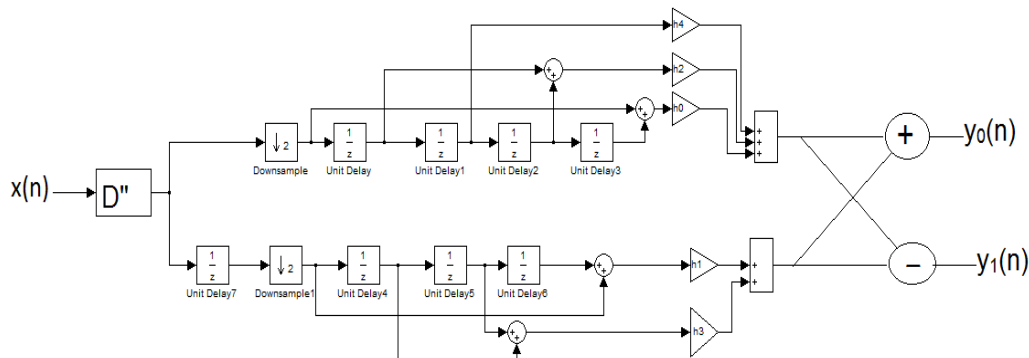Fig. 7 The magnitude and phase responses of $H(e^{j\omega})$ with (σ = 1).

Fig.8 The final lattice FIR wavelet filter bank structure with (σ = 1).

b) A Multiplierless Realization

The rounded values of the resulting scaled coefficients for different wordlengths are illustrated in Table 1.

Table 1 The rounded coefficient values for different wordlengths.

Wordlength (bits) / Original Coefficient	Coefficients for different wordlengths							
	3	4	5	6	7	8	9	10
0.0017	0	0	0	0	0	0	0	9.7656e-4
0.0169	0	0	0	0.0156	0.0156	0.0156	0.0156	0.0166
0.0870	0	0.0625	0.0625	0.0781	0.0859	0.0859	0.0859	0.0869
0.2328	0.1250	0.1875	0.2188	0.2188	0.2266	0.2305	0.2324	0.2324
0.3231	0.2500	0.3125	0.3125	0.3125	0.3203	0.3203	0.3223	0.3223

The approximated values of Table 1 are used in a Matlab simulation for best selection of maximum and average error values in the resulting filter magnitude response and the

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resulting SNR values.Calculations ofthe values of average error and deviation are carried out by following equations:

$$\Delta_{avg} = (1/m) * \sum_1^m \Delta\left(e^{j\omega}\right)$$

$$m = length\ of\ \left(H_0\left(e^{j\omega}\right)\right) = \text{no. of frequency samples} \qquad \qquad …(8)$$

$$\Delta\left(e^{jw}\right) = \left|H_{original}\left(e^{j\omega}\right) - H_{wordlength}\left(e^{j\omega}\right)\right|$$

$$Deviation = 1 - max\left\{H_{wordlength}\left(e^{j\omega}\right)\right\}$$

where:

$H_{original}\left(e^{jw}\right)$ is the original frequency response.

$H_{wordlength}\left(e^{jw}\right)$ is the frequency response at a specified wordlength.

$Deviation$ is the amount of error in the frequency response at any wordlength.

From equation (8), Table 2 is obtained. It will lead us to the corrected choice for coefficients word lengths. It can be seen in Table 2 that, a wordlength of 6 bits can be chosen for acceptable values of average error and deviation. Also, Table 3 returns the suitable number of ECG samples for a maximum SNR valueof 37.0606dB.

Table 2 Maximum and average deviations.

Wordlength (bits)	3	4	5	6	7	8	9	10
Δ_{avg}	0.1450	0.0599	0.0329	0.0177	0.0079	0.0035	0.0027	0.0011
$H_{wordlength}$	0.5	0.8125	0.8751	0.9375	0.9765	0.9843	0.9901	0.9961
$Deviation$	0.5	0.1875	0.1249	0.0625	0.0235	0.0157	0.0099	0.0039

Table 3 SNR values with respect to no. of samples for the input ECGsignal.

Wordlength (bits) / No.of Samples	SNR values in (dB) for different wordlengths (in bits)							
	3	4	5	6	7	8	9	10
20	18.7795	28.7430	29.8735	37.0606	40.2516	52.7677	53.2702	61.0592
40	18.7832	29.8413	31.8251	35.9911	45.4214	54.8581	51.5275	65.1076
60	16.6328	26.9843	31.9761	34.8170	44.3359	51.0628	52.7310	60.4078
80	16.6352	26.6825	31.4614	34.9883	44.6972	50.7150	53.2873	61.8624
100	15.2283	24.7151	29.9835	33.4573	42.7649	49.0411	54.5575	61.5493
120	15.2015	24.7018	29.3972	33.5001	43.0360	48.3479	54.7324	61.1366
140	15.2296	24.4127	29.2695	33.4544	42.7619	49.9888	54.5697	61.5065
160	15.6710	24.6147	29.2656	33.8426	42.9003	47.8922	54.0714	61.3886
180	16.1534	25.1310	29.4137	34.3439	43.4716	48.0435	53.7406	61.2532
200	16.6931	25.6434	29.7235	34.8739	43.9559	48.2593	53.5781	61.1686

From Table 3, the 6-bit representation tolerates a suitable number of ECG samples of 20 samples for the pre mentioned maximum SNR value. Since the FIR filter response is

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symmetric, therefore the number of multipliers can be reduced to almost half of its original value($1 + 4\sigma$). Thus, only5 multipliers can be used in the realization of such filter banks. From Table 1 and for 6-bit representations, the exact number of required multipliers appears to be reduced to 4. In addition, these 4 multipliers can be represented in sum-of-power-of-two (SOPOT) resulting in a multiplier less realizations shown in Table 4.Hardwarely speaking, a limited number of shifters and adders or subtracts are needed.

Table 4, Multiplier less representation of coefficients.

6-bit representation of coefficients	SOPOTrepresentation of coefficients
$h_0 = 0$	None
$h_1 = 0.0156$	2^{-6} = six shifts only
$h_2 = 0.0781 = 0.0625 + 0.0156$	$2^{-4} + 2^{-6}$ = shift and add
$h_3 = 0.2188 = 0.2500 - 0.03125$	$2^{-2} - 2^{-5}$ = shift and subtract
$h_4 = 0.3125 = 0.2500 + 0.0625$	$2^{-2} + 2^{-4}$ = shift and add

IV. Gaussian FIRWavelet Filter with $\sigma = 2$
a) Lattice Structure

The same procedure of the previous section can also be followed. The filter response of $H(z)$ will have 17 coefficients with the following system function that corresponds to the samples of Fig. 9 which represent a sampled version of the original mother wavelet function with $\sigma = 2$:

$$H(z) = h_0 + h_1 z^{-1} + h_2 z^{-2} + h_3 z^{-3} + h_4 z^{-4} + h_5 z^{-5} + h_6 z^{-6} + h_7 z^{-7} + h_8 z^{-8} + h_9 z^{-9} + h_{10} z^{-10} + h_{11} z^{-11} + h_{12} z^{-12} + h_{13} z^{-13} + h_{14} z^{-14} + h_{15} z^{-15} + h_{16} z^{-16} \qquad \ldots(9)$$
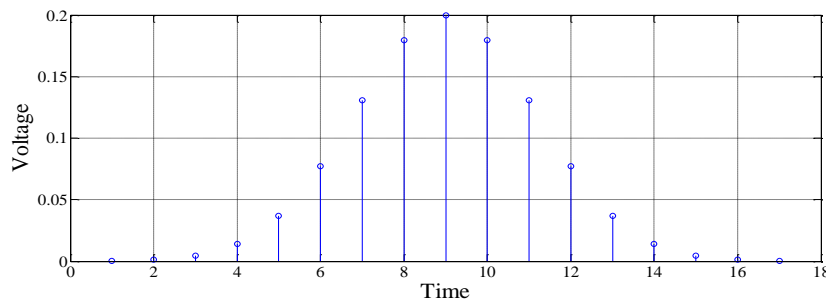

Fig. 9Impulse response of Gaussian function with (σ = 2).

By the same property of quadrature mirror filters (QMFs), $G(z) = H(-z)$, the system function $G(z)$ that corresponds to the scaling function can be written as

$$G(z) = h_0 - h_1 z^{-1} + h_2 z^{-2} - h_3 z^{-3} + h_4 z^{-4} - h_5 z^{-5} + h_6 z^{-6} - h_7 z^{-7} + h_8 z^{-8} - h_9 z^{-9} + h_{10} z^{-10} - h_{11} z^{-11} + h_{12} z^{-12} - h_{13} z^{-13} + h_{14} z^{-14} - h_{15} z^{-15} + h_{16} z^{-16} \qquad \ldots(10)$$

The filters' polyphase representations can then be expressed by

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$$H_{even}(z^2) = h_0 + h_2z^{-2} + h_4z^{-4} + h_6z^{-6} + h_8z^{-8} + h_{10}z^{-10} + h_{12}z^{-12} + h_{14}z^{-14}$$
$$+ h_{16}z^{-16}$$
$$H_{odd}(z^2) = h_1 + h_3z^{-2} + h_5z^{-4} + h_7z^{-6} + h_9z^{-8} + h_{11}z^{-10} + h_{13}z^{-12} + h_{15}z^{-14}$$

$$\text{...(11)}$$

The down-sampled form of equation (11) is written as

$$H_{even}(z) = h_0 + h_2z^{-1} + h_4z^{-2} + h_6z^{-3} + h_8z^{-4} + h_{10}z^{-5} + h_{12}z^{-6} + h_{14}z^{-7} + h_{16}z^{-8}$$
$$H_{odd}(z) = h_1 + h_3z^{-1} + h_5z^{-2} + h_7z^{-3} + h_9z^{-4} + h_{11}z^{-5} + h_{13}z^{-6} + h_{15}z^{-7}$$

$$\text{...(12)}$$

Therefore,
$$H(z) = H_{even}(z) + z^{-1}H_{odd}(z)$$
and
$$G(z) = H_{even}(z) - z^{-1}H_{odd}(z)$$

$$\text{... (13)}$$

with the following coefficients values:

$h_0 = h_{16} = 0.0002$, $h_1 = h_{15} = 0.0011$, $h_2 = h_{14} = 0.0044$, $h_3 = h_{13} = 0.0142$, $h_4 = h_{12} = 0.0367$, $h_5 = h_{11} = 0.0770$, $h_6 = h_{10} = 0.1306$, $h_7 = h_9 = 0.1794$ and $h_8 = 0.1995$.

Using the same previous scaling procedure, the value of α for [
$|H(e^{j\omega})| \leq 1$] turns to be 0.9201. Therefore, the new scaled coefficients values are:

$h_0 = h_{16} = 0.0002$, $h_1 = h_{15} = 0.0010$, $h_2 = h_{14} = 0.0041$, $h_3 = h_{13} = 0.0130$, $h_4 = h_{12} = 0.0338$, $h_5 = h_{11} = 0.0708$, $h_6 = h_{10} = 0.1202$, $h_7 = h_9 = 0.1651$ and $h_8 = 0.1835$.

In this stage of design, the number of coefficients islimited to9 due to symmetry property. The resulting magnitude and phase responses of $H(e^{j\omega})$ of the system function in equation (13),are shown in Fig. 10. The final lattice structure in Matlab simulation is shown in Fig. 11.
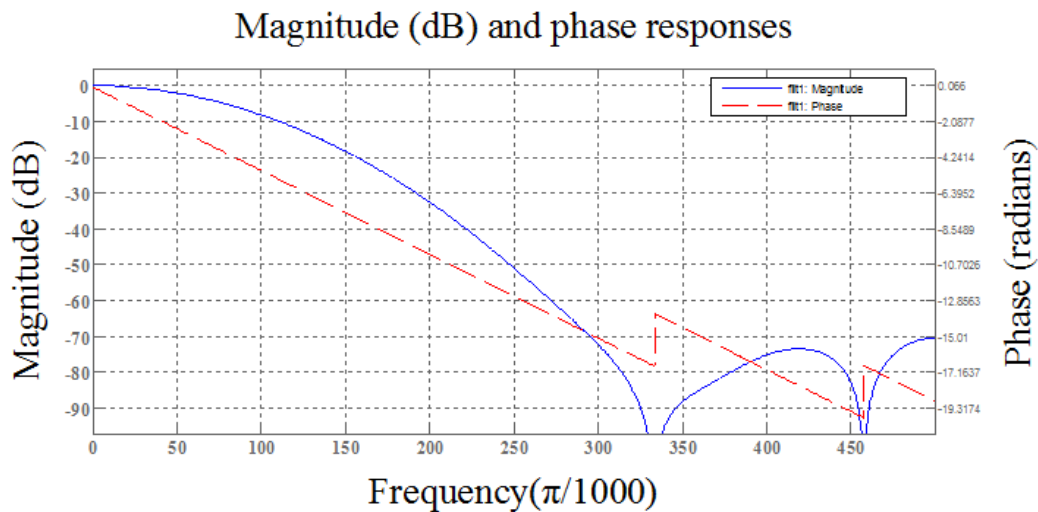

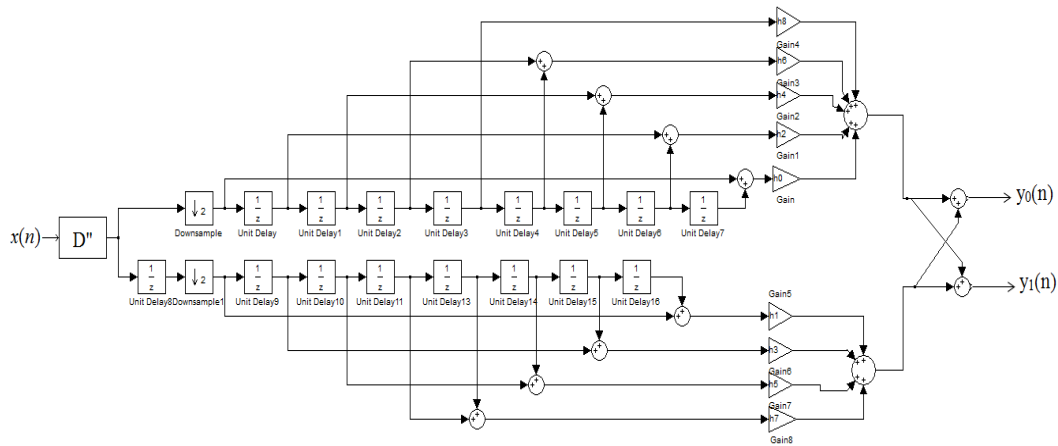Fig. 10 The magnitude and phase responses of $H(e^{j\omega})$ with (σ = 2).

Fig. 11 The final lattice FIR wavelet filter bank structure with (σ = 2).

b) A Multiplierless Realization

By the same previous procedure, awordlength of 6 bitscan also be chosen where the maximum and average deviations are acceptable (maximum error is 0.0389& average deviation is 0.0088) and the maximum SNR value is 46.2504dBat an ECG number of samples of 20. Using 6-bit representations, the exact number of required multiplierscan further be reduced to5. In addition, such multipliers can be represented in SOPOT, resulting in a multiplierless realizationas shown in Table 5.

Table 5 Multiplierless representation of coefficients.

6-bit representation of coefficients	SOPOT representation of Coefficients
$h_0 = h_1 = h_2 = h_3 = 0$	**None**
$h_4 = 0.0313$	2^{-5} = **Five shifts (a shifter only)**
$h_5 = 0.0625$	2^{-4} = **Four shifts (a shifter only)**
$h_6 = 0.1094 = 0.1250 - 0.0156$	$2^{-3} - 2^{-6}$ = **shift and subtract**
$h_7 = 0.1563 = 0.1250 + 0.0313$	$2^{-3} + 2^{-5}$ = **shift and add**
$h_8 = h_5 + h_6 = 0.1719$	$2^{-3} + 2^{-4} - 2^{-6}$ = **shift, add and subtract**

V. ECG Feature Extraction

This section exhibits the data types of ECG signal which are adopted as input signals to the designed systems. The data represents a group of diseases in addition to the normal state.

The extracted feature from the ECG signal plays a vital role in diagnosing the cardiac disease. Therefore, it is necessary that the feature extraction system performs accurately. The purpose of feature extraction is to find as few properties as possible within ECG signal that would allow successful abnormality detection and efficient prognosis. To get the feature vector for any ECG signal, the concantination of the wavelet coefficients of the last scale level and some scaling coefficients is usually obtained [6]. In this paper, the concantination of the third or secondlevel wavelet and scaling coefficients is used to form the feature vector in each tested ECG signal. These vectors (in hexadecimals) are illustrated in Tables 6 and 7 for both standard deviation values$\sigma = 1$ and $\sigma = 2$,respectively.

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Table 6 Wavelet and scaling coefficients (three-level) of tested ECG signals with σ =1.

Normal ECG signal	Wavelet coef.	0	1	FC	FD	7	FF	0	2	0	0
	Scaling coef.	0	FF	5	6	4	0	5	4	0	0
Bradycardia ECG signal	Wavelet coef.	0	0	0	1	2	FF	2	FC	0	0
	Scaling coef.	0	0	FD	FD	1	0	FC	F7	2	0
Tachycardia ECG signal	Wavelet coef.	1	1	0	FB	FC	7	6	1	FC	FF
	Scaling coef.	0	FF	FF	1	9	F	FA	F5	FD	FF
Hyperkalemia ECG signal	Wavelet coef.	0	0	0	3	3	1	1	FE	FC	0
	Scaling coef.	0	0	FE	FA	FC	F9	EF	F4	FD	0
WPW syndrom ECG signal	Wavelet coef.	0	FF	0	0	1	4	FF	FE	0	0
	Scaling coef.	0	2	4	5	FF	0	FA	FA	2	0
Pacemaker ECG signal	Wavelet coef.	0	0	FE	1	0	1	3	FF	0	0
	Scaling coef.	0	0	FF	7	8	1	FF	FF	0	0
Established angina ECG signal	Wavelet coef.	0	0	FC	2	2	1	FD	FF	3	1
	Scaling coef.	0	FF	6	C	4	3	FD	3	5	1

Table 7 Wavelet and scaling coefficients (two-level) of tested ECG signals with σ =2.

Normal ECG signal	Wavelet coef.	0	1	3	2	FD	FA	FC	FE	FE	0	3	3	3	2	1	0	0
	Scaling coef.	0	FF	FF	1	3	0	FE	1	0	FE	FF	1	0	0	1	0	0
Bradycardia ECG signal	Wavelet coef.	0	FF	FD	FC	FD	1	4	4	4	4	2	FE	FA	FE	2	2	1
	Scaling coef.	0	1	1	0	FE	FF	0	1	1	0	1	3	0	FD	FF	1	1
Tachycardia ECG signal	Wavelet coef.	1	1	2	3	2	FC	F9	FD	6	6	FE	F9	FB	3	5	2	0
	Scaling coef.	0	0	0	0	2	3	1	FB	FC	2	5	2	FC	FD	1	2	0
Hyperkalemia ECG signal	Wavelet coef.	0	FF	FD	FD	FD	FF	1	6	7	3	FD	FA	FD	2	3	1	0
	Scaling coef.	0	1	1	FF	FF	0	FE	FE	1	3	3	1	FD	FE	1	1	0
WPW syndrom ECG signal	Wavelet coef.	0	1	1	1	2	1	FE	FB	0	4	3	FE	FB	FF	3	2	1
	Scaling coef.	0	0	0	0	FF	0	3	0	FD	FE	1	4	0	FD	FF	1	1
Pacemaker ECG signal	Wavelet coef.	0	FE	FC	FC	FF	4	7	5	FF	FC	FF	1	2	1	0	0	0
	Scaling coef.	0	1	1	0	FE	FD	FF	3	3	0	FE	FF	0	1	0	0	0
Established angina ECG signal	Wavelet coef.	FF	FD	FF	4	6	1	0	4	3	FF	FC	FC	FD	FE	0	1	1
	Scaling coef.	1	1	FE	FD	2	3	FF	FF	2	2	0	FF	0	FF	FF	0	1

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VI.   Conclusions

ECG-based FIR wavelet filter banks have been designed. The Gaussian function has been utilized as a mother wavelet function stage withan advancing difference stage. Sampled versions of such wavelet function are used as impulse responses to the designed wavelet filter banks. These banks have been realized in a highly-efficient lattice structures which are easy to implement. The numbers of filter banks coefficients have been reduced to more than half of their original values. Resulting in reducing the number of multiplications and improving the filter banks efficiencies as the final number of computationsperformed is reduced. This may lead to less-complex hardware implementations. SOPOT method has been applied to quantized different multiplier values, leading to multiplierless realizations for such multiplier values (shift and add only).

In spite of the need for at least more than one level wavelet decompositions for ECG-QRS feature extraction, the proposed lattice structures can also serve for that purpose because of their less-complex and computational-efficient realizations.

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